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# Probabilistic Time Consistent Queries over Moving Objects

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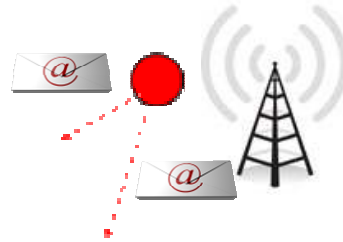
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# Motivation Example

- Delay Tolerance Network (DTN)

**mobile node**

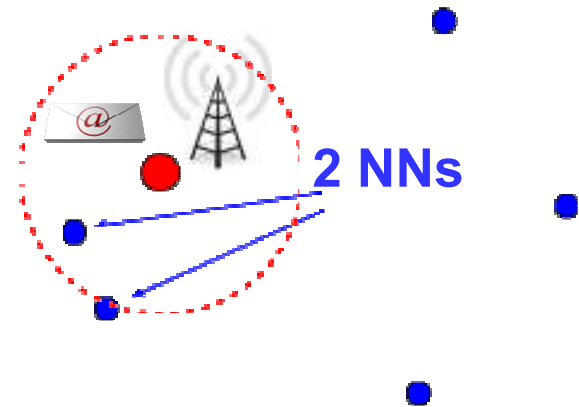
**base station**



# Motivation Example (cont'd)

- Delay Tolerance Network (DTN)
  - A base station transmits a message to passing mobile nodes
  - Due to the limited bandwidth, the base station only sends message to its closest mobile nodes
  - It takes some time to send the message (e.g. audios/videos)

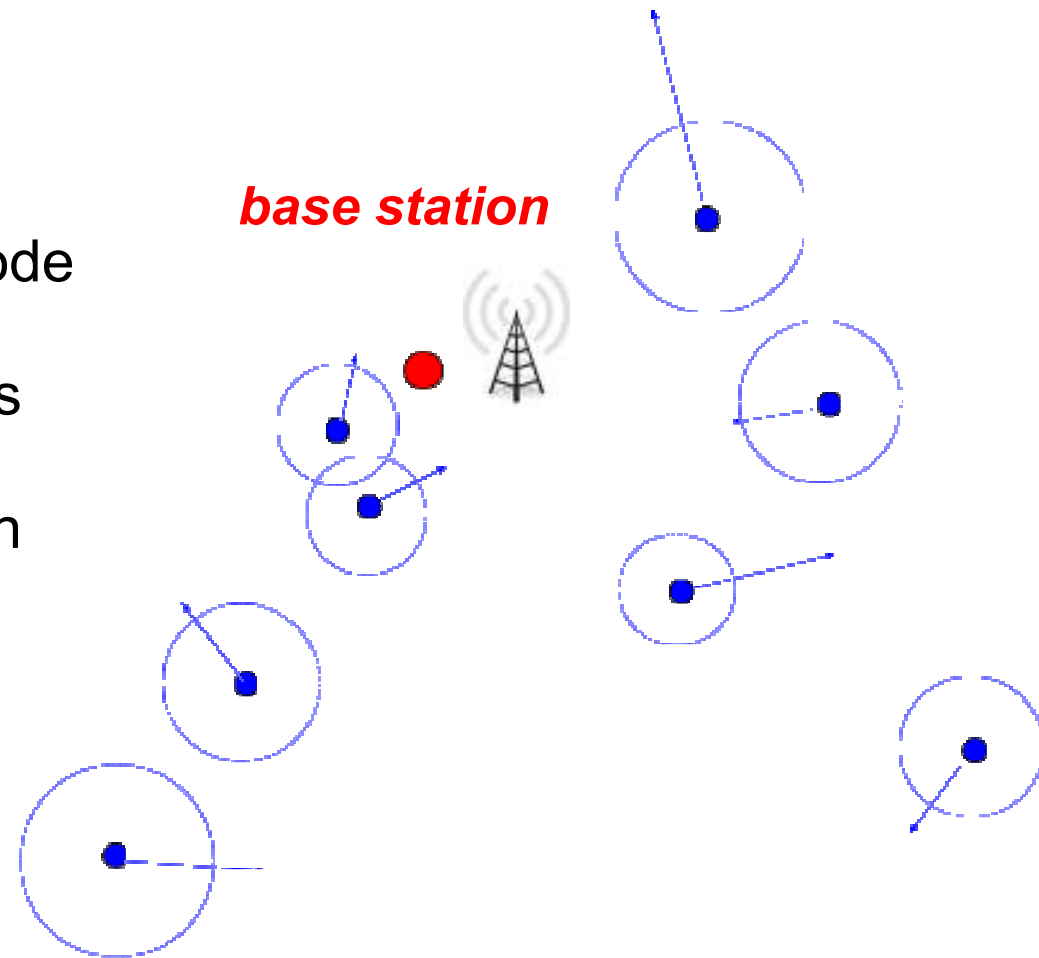
**base station**



- Find those mobile nodes that are *consistently* being  $k$ -nearest neighbors of a base station for at least  $T$  consecutive timestamps in a future period  $[0, ted]$

# Motivation Example (cont'd)

- Delay Tolerance Network (DTN)
  - The location of each mobile node can be imprecise due to the accuracy of positioning devices
  - Conduct *probabilistic time consistent queries* on uncertain moving objects *efficiently* and *effectively*



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# Outline

- Introduction
- Data Model
- Problem Definition
- The Proposed Approaches
- Experimental Results
- Conclusions

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# Introduction

- Data uncertainty is ubiquitous in many real-world applications
  - Sensor networks
  - Location-based services
  - Moving object search
  - Privacy preserving
- Reasons
  - Imperfect nature of sensing devices
  - Noises added to data during the data transmission
  - Intentional perturbation for privacy preserving

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# Uncertainty Model for Uncertain Moving Objects

# Definition of Probabilistic Time Consistent Queries

- Probabilistic Time Consistent Queries (PTCQ) on Uncertain Moving Objects
  - An uncertain moving object database,  $DU$
  - A query point  $q$
  - A time threshold  $T$
  - A future period  $[0, ted]$  ( $ed + 1 \leq T$ )
  - A probabilistic threshold  $a$
  - A PTCQ query retrieves uncertain objects  $o \in DU$  such that  $o$  are in the  $k$ NN set of  $q$ ,  $PkNN(ti)$ , for *all* timestamps  $ti \in [tj, tj+T-1] \subseteq [0, ted]$ , with  $k$ NN probability greater than or equal to  $a$  at each timestamp

$$PTCQ(t_i) = \bigcup_{t_j=0}^{t_{ed}-T+1} \left( \bigcap_{t_i=t_j}^{t_j+T-1} PkNN(t_i) \right)$$



# Con- $k$ NN Definition (cont'd)

- A probabilistic  $k$ -nearest neighbor (PkNN) query retrieves uncertain objects of being  $k$ -nearest neighbor of a query point  $q$  with  $k$ NN probability  $Pr_{kNN}(q, o, t_i) \square a$

$$\begin{aligned}
 & Pr_{kNN}(q, o(t_i)) \\
 = & \int_{v_o^-}^{v_o^+} pdf_v(v_o) \cdot \int_{o'(t_i) \in UR(o(t_i))} Pr\{dist(q, o'(t_i)) = r\} \\
 & \cdot \sum_{\forall S = \{p_1(t_i), \dots, p_s(t_i)\} \in \mathcal{D}^U \wedge s < k} \left( \left( \prod_{m=1}^s Pr\{dist(q, p_m(t_i)) < r\} \right) \right. \\
 & \left. \cdot \left( \prod_{p_n \in \mathcal{D}^U \setminus (S \cup \{o\})} Pr\{dist(q, p_n(t_i)) \geq r\} \right) \right) do'(t_i) dv_o
 \end{aligned}$$

# Pruning Heuristics

- Assume we can obtain  $k$  objects  $o_1, o_2, \dots, o_k$ , close to query point  $q$
- In future period  $[0, ted]$ , the maximum distance,  $R_{max}$ , from these  $k$  objects to  $q$ , is given by:
  - $R_{max} = \max_j \{ \text{dist}(q, o_j(0)), \text{dist}(q, o_j(ted)) \mid 1 \leq j \leq k \}$
- Any object intersecting with  $\mathcal{H}$  is a PTCQ candidate

# Pruning Techniques

- Basic idea
  - If an uncertain object  $o$  of being  $PkNN$  only last for less than  $T$  consecutive timestamps in future period  $[0, ted]$ , then object  $o$  can be safely pruned
- Pruning methods
  - $T$ -pruning
  - Period pruning
  - Segment pruning

# T-Pruning

- The trajectory of  $o$  should intersect with circle centered at  $q$  with radius  $R_{max}$  having length at least  $v_o \square T$

*T-pruning  
condition:*

$$\|q\| \cdot \cos(\eta_q - \gamma) < C_o[x] \cdot \cos\gamma + C_o[y] \cdot \sin\gamma, \text{ or}$$

$$\|q\| \cdot \sin(\gamma - \eta_q) - (C_o[x] \cdot \sin\gamma - C_o[y] \cdot \cos\gamma) > (R_{max} + r_o)^2 - (v_o^- \cdot T)^2 / 4.$$

# Period Pruning – Case 1

- Object  $o$  is initially outside

*Period pruning  
condition:*

$$\|q\| \cdot \cos(\eta_q - \gamma) - (C_o[x] \cdot \cos\gamma + C_o[y] \cdot \sin\gamma) < \frac{v_o^{+2} \cdot (t_{ed} - T)^2 - (R_{max} + r_o)^2 + \text{dist}^2(q, C_o)}{2 \cdot v_o^{+2} \cdot (t_{ed} - T)}$$

# Period Pruning – Case 2

- Object  $o$  is initially intersecting with

*period pruning  
condition:*

$$\|q\| \cdot \cos(\eta_q - \gamma) - (C_o[x] \cdot \cos\gamma + C_o[y] \cdot \sin\gamma) < \frac{v_o^{-2} \cdot T^2 - (R_{max} + r_o)^2 + dist^2(q, C_o)}{2 \cdot v_o^{-2} \cdot T}$$

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# Segment Pruning

- Observation:  $R_{max}$  might vary over time

# Utilize Velocity and Object Distributions

- Filtering with velocity distributions
  - Replace  $v_{o-}$  and  $v_{o+}$  with  $v_{omin}$  and  $v_{omax}$ , respectively, such that:  
 $v_{omin} = v_{o-} - b$ , where  $b < a$
- Filtered velocity distributions  
$$\int_{v_{omin}^{1-\beta}}^{v_{omax}^{1-\beta}} pdf_v(v_o) dv_o = 1 - \beta$$



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# Indexing

- *UC-Grid* Index

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# PTCQ Query Processing

- Find influence region of  $q$ 
  - $V_{max}$  – global maximum velocity
- For cells intersecting with the influence region
  - Apply pruning methods
- The remaining candidates are refined

# Experimental Evaluation

- Experimental Settings
  - Real data: *CA* (California spatial data set)
  - Synthetic data: *IUrU*, *IUrG*, *ISrU*, and *ISrG*
    - Velocity  $v_0$  is randomly generated within  $[Vmin, Vmax]$
  - Competitor:
    - *Basic* method: first compute *PkNN* answers at each timestamp via *UC-Grid* index, and then combine the *PkNN* results
  - Measures:
    - Filtering time through *UC-Grid* index
    - Speed-up ratio compared with *Basic*

# Performance vs. $a$

***IU data sets***

***IS data sets***

*data size  $N = 30K$ , radius range  $[rmin, rmax] = [0, 0.0005]$ ,  $T = 8$ ,  $[0, ted] = [0, 20]$ ,  $[Vmin, Vmax] = [0, 0.001]$ , and  $k = 10$*

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# Conclusions

- We formulate the problem of probabilistic time consistent query (PTCQ). In particular, we consider PTCQ with probabilistic time consistent  $k$ NN query
- We propose 3 effective pruning methods and 2 probabilistic filtering approaches to reduce the search space
- We design the grid index for storing uncertain moving objects and present efficient query processing approach
- We demonstrate the efficiency of our proposed query answering approaches

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# Thank you!

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**Q/A**